

**Guided Exercises / Practical Work 2***Today's effort becomes tomorrow's wisdom***Exercise 1: E-Commerce Platform Development**

Your team is building a full-stack e-commerce platform with product catalog, shopping cart, payment gateway, and admin dashboard.

**Project Activities**

ID	Activity	Duration (Days)	Predecessor(s)
A	Market Research & Requirements	5	—
B	System Architecture Design	4	A
C	Database Schema Design	3	B
D	Product Catalog Module	6	C
E	User Authentication Module	4	C
F	Shopping Cart & Checkout	7	D, E
G	Payment Gateway Integration	5	F
H	Admin Dashboard	4	D
I	System Integration & API Testing	4	G, H
J	User Acceptance Testing (UAT)	3	I
K	Production Deployment	2	J

**Questions****Part 1 – A. Network Diagram**

- Draw the PERT network diagram (activity-on-node format).
- List all possible paths from start to finish.
- Identify the longest path visually.

**Part 2 – B. Time Analysis**

- Calculate ES (Earliest Start) and EF (Earliest Finish) for each activity.
- Calculate LS (Latest Start) and LF (Latest Finish) for each activity.
- Compute Slack Time ( $Slack = LS - ES$ ) for each activity.

**Part 3 – C. Critical Path**

- Identify the critical path(s).
- What is the minimum project duration?
- Which activities have zero slack?

**Part 4 – D. Risk Analysis**

- If activity **F** (Shopping Cart) is delayed by 3 days, does the project finish date change? Justify.

- (b) If activity **H** (Admin Dashboard) finishes 2 days early, can the project finish earlier? Why or why not?
- (c) Why is slack time important for project managers when allocating resources?

### Bonus Challenge (Advanced)

Assume three-time estimates for each activity. Using the PERT formula:

$$T_E = \frac{O + 4M + P}{6}$$

Calculate expected durations and variance ( $\sigma^2 = \left(\frac{P-O}{6}\right)^2$ ). Then:

- Recalculate the critical path using  $T_E$
- Compute the probability that the project finishes within 35 days (use normal distribution approximation)

### Exercise 2: AI-Powered Recommendation Engine

**Context:** Your startup is developing a machine learning recommendation system for a streaming platform (movies/music).

#### Project Activities

ID	Activity	Duration (Days)	Predecessor(s)
A	Data Collection & Cleaning	6	—
B	Feature Engineering	5	A
C	Model Selection & Prototyping	4	B
D	Training Pipeline Development	7	C
E	Evaluation Framework	3	C
F	A/B Testing Infrastructure	5	D, E
G	Real-time API Development	6	D
H	Dashboard for Analytics	4	E
I	Model Deployment & Monitoring	3	F, G, H
J	Performance Optimization	4	I

#### Questions

##### Part 1 – A. Network Analysis

- (a) Draw the PERT diagram.
- (b) How many merge points (nodes with multiple incoming arrows) exist? Why are they risky?

##### Part 2 – B. Forward & Backward Pass

- (a) Perform forward pass to compute ES/EF.

- (b) Perform backward pass to compute LS/LF.
- (c) Tabulate all values in a single table.

### Part 3 – C. Critical Path & Float

- (a) Identify critical path(s).
- (b) Which activity has the largest slack? What does this mean for scheduling flexibility?
- (c) If two critical activities run in parallel, how does this affect risk management?

### Part 4 – D. Agile Considerations

- (a) In Agile development, would you still use PERT? Justify your answer.
- (b) How would you adapt this PERT analysis for 2-week sprints?

## Bonus Challenge (Advanced)

Introduce resource constraints: only 2 ML engineers available. Activities D, E, G require 1 engineer each; F requires 2 engineers simultaneously.

- Identify resource conflicts on the critical path
- Propose a feasible schedule respecting constraints (without changing dependencies)

## Exercise 3: IoT Smart Home System

**Context:** Your team is developing an IoT platform connecting sensors (temperature, motion, cameras) to a central hub with mobile app control.

### Project Activities

ID	Activity	Duration (Days)	Predecessor(s)
A	Hardware Specification	4	—
B	Sensor Firmware Development	8	A
C	Hub Firmware Development	7	A
D	Cloud Backend Architecture	5	A
E	Device-to-Cloud Protocol	6	B, C, D
F	Mobile App UI Design	4	D
G	Mobile App Development	9	E, F
H	Security & Encryption Layer	5	E
I	End-to-End Integration Testing	6	G, H
J	Beta Testing with Users	5	I
K	Certification & Compliance	7	J
L	Mass Production Setup	4	K

## Questions

### Part 1 – A. Complex Dependencies

- (a) Draw the PERT diagram (note: activity E has **three** predecessors).
- (b) Identify all paths and their total durations.

### Part 2 – B. Time Calculations

- (a) Compute ES, EF, LS, LF for all activities.
- (b) Create a table showing Duration, ES, EF, LS, LF, and Slack for each activity.

### Part 3 – C. Critical Path Analysis

- (a) What is the critical path? Highlight it in red on your diagram.
- (b) What is the total project duration?
- (c) If activity **H** (Security) is delayed by 4 days, what happens to the project end date?

### Part 4 – D. Hardware-Software Co-design

- (a) Why is activity E (Protocol) a high-risk bottleneck?
- (b) How would you mitigate risk for activities with multiple predecessors?
- (c) In embedded systems projects, why is the critical path often dominated by hardware dependencies?

## Bonus Challenge (Advanced)

Assume optimistic/pessimistic estimates. After computing  $T_E$ :

- Calculate the standard deviation of the critical path
- Determine the project duration with 95% confidence level ( $Z = 1.645$ )

## Exercise 4: Cross-Platform Mobile Health App

**Context:** Your team is building a health tracking app (iOS/Android) with wearable integration, data visualization, and telemedicine features.

## Project Activities

ID	Activity	Duration (Days)	Predecessor(s)
A	Regulatory Requirements Analysis	5	—
B	UX/UI Wireframing	4	A
C	iOS Development	10	B
D	Android Development	10	B
E	Wearable API Integration	6	C, D
F	Backend Microservices	8	A
G	Data Visualization Engine	5	F
H	Telemedicine Module	7	F
I	HIPAA Compliance Implementation	6	E, G, H
J	Clinical Validation Testing	8	I
K	App Store Submission & Review	5	J

## Questions

### Part 1 – A. Parallel Development

- Draw the PERT diagram. Note the parallel iOS/Android tracks.
- How does parallel development affect the critical path?

### Part 2 – B. Time Analysis

- Compute ES/EF using forward pass.
- Compute LS/LF using backward pass.
- Identify activities with positive slack.

### Part 3 – C. Critical Path & Sensitivity

- What is the critical path? Is it unique?
- If iOS development (C) finishes 2 days early but Android (D) is delayed by 3 days, what is the net impact?
- Why might regulatory activities (A, I) be critical even with moderate duration?

### Part 4 – D. Real-World Constraints

- App Store review (K) has variable duration (310 days). How would you model this uncertainty?
- Why is clinical validation (J) often a project bottleneck in health tech?
- Propose 2 strategies to compress the project schedule without adding resources.

**Bonus Challenge (Advanced)**

**Crashing Analysis:** Management demands 5-day schedule compression. Given crash costs:

Activity	Crash Cost (\$/day)
C/D (Mobile Dev)	\$800
F (Backend)	\$600
J (Validation)	\$1,200
K (Submission)	Not crashable

- Which activities should be crashed to minimize cost?
- What is the minimum cost to achieve 5-day compression?